

and mutual interaction of short-chain radicals, especially if these occur in regions of high local radical concentration.

**Acknowledgments.** We wish to thank the Australian Institute of Nuclear Science and Engineering for

supporting this project, the Australian Atomic Energy Commission, and particularly Mr. J. H. Bolton and Mr. B. M. O'Leary, for irradiation of samples, Professor L. E. Lyons for generously making the esr facilities available, and C.S.I.R.O. for providing a studentship for M. J. B.

## Interactions in Solutions of Block and Statistical Copolymers of Styrene and Methyl Methacrylate

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Received August 30, 1968

**ABSTRACT:** Intrinsic viscosities of block and statistical copolymers of styrene (S) and methyl methacrylate (M) are analyzed as a function of molecular weight and composition by means of relations recently applied to styrene–butadiene block polymers. The unperturbed dimensions of the block polymer are entirely determined by those of the individual blocks and the composition. In the statistical copolymers they depend on the placement probabilities of the various pairs along the chain, but the departure from the relation for block copolymers turns out to be small. The long-range interaction parameter can be expressed for both types of copolymers as a quadratic form in the composition. The polymer–polymer interaction factor varies with the polymerization conditions of the PMMA block, and a correlation with the heterotacticity index is shown to exist. In a series of samples with similar indices for heterotacticity the interaction parameter is independent of molecular weight, composition and number of blocks. Also, no systematic differences are observed between benzene and toluene at 25 and 30°.

The solution properties of block copolymers have been investigated for a number of years and the poly(methyl methacrylate) (PMMA)–polystyrene (PS) combination has been a preferred object of study. Frequently contradictory findings have been summarized at various occasions.<sup>2–9</sup>

We have recently measured the intrinsic viscosities and second virial coefficients of polystyrene–polybutadiene block copolymers<sup>10</sup> and given a description of the molecular weight and composition dependence. It is based on the concept of a  $\theta$  temperature at which all long-range interactions vanish separately rather than on a mutual compensation which would make the  $\theta$  temperature dependent on molecular weight and composition for a given solvent.<sup>8,11,12</sup> The purpose

of this paper is to examine available experimental data on PS–PMMA di- and triblock copolymers on the basis of the relations developed previously.

### Method of Analysis

Consider a block copolymer composed of a series of chemical species  $i = 1, 2, \dots, n$ . Let  $M_i$  be the molecular weight of species  $i$ , with a repeat unit of molecular weight  $M_{0i}$  (per one carbon bond of the backbone chain), unperturbed dimensions  $\langle r_0^2 \rangle_i$ , and short-range interaction parameter  $A_i^2 = a_i^2/M_{0i} = \langle r_0^2 \rangle_i/M_i$ . If  $x_i$  is the mole fraction and  $B_i = \beta_i/M_{0i}^2$  the long-range interaction parameter, we write for the copolymer the averages<sup>10</sup> given in eq 1, where the subscript  $c$  refers to the copolymer. The second equation

$$M_{0c} = \sum_i x_i M_{0i}$$

$$a_c^2 = A_c^2 M_{0c} = \sum_i x_i a_i^2 \quad (1)$$

$$\beta_c = B_c M_{0c}^2 = \sum_i \beta_i x_i^2 + 2 \sum_{i < j} \beta_{ij} x_i x_j$$

expresses the Gaussian character of the chain at  $T = \theta$ , where all  $\beta_{ij}$  vanish. The third assumes that the fraction of  $i$ – $j$  configurations characterized by an interaction parameter  $\beta_{ij}$  can be represented as a product of mole fractions. This, of course, is strictly valid only for a random distribution of segments, and should not be expected to hold if all the  $\beta$ 's are sufficiently different from each other. In the styrene–butadiene system, eq 1 proved to be valid in solvents which are good for at least one of the components.<sup>10</sup> Equation 1 extends any two-parameter (A,B) relation developed for homopolymers to block copolymers by the introduction of additional quantities  $\beta_{ij}$ .

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(2) (a) G. M. Burnett, P. Meares, and C. Paton, *Trans. Faraday Soc.*, **58**, 737 (1962); (b) S. Krause, *J. Phys. Chem.*, **68**, 1948 (1964).

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(4) W. H. Stockmayer, L. D. Moore, Jr., M. Fixman, and B. N. Epstein, *J. Polym. Sci.*, **16**, 517 (1955).

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(8) H. Inagaki and Y. Miyamoto, *Makromol. Chem.*, **87**, 166 (1965).

(9) H. Inagaki, *ibid.*, **86**, 298 (1965).

(10) L. Utracki and R. Simha, *Amer. Chem. Soc., Div. Polym. Chem., Preprints*, **9**, 742 (1968); L. Utracki, R. Simha, and L. J. Fetters, *J. Polym. Sci., Part A-2*, in press. For the second virial coefficient of a statistical copolymer, a quadratic form in the composition (see eq 1) was given earlier by R. Simha and H. Branson, *J. Chem. Phys.*, **12**, 253 (1944).

(11) S. Schlick and M. Levy, *J. Phys. Chem.*, **64**, 883 (1960).

(12) T. Kotaka, H. Ohnuma, and Y. Murakami, *ibid.*, **70**, 4099 (1966).

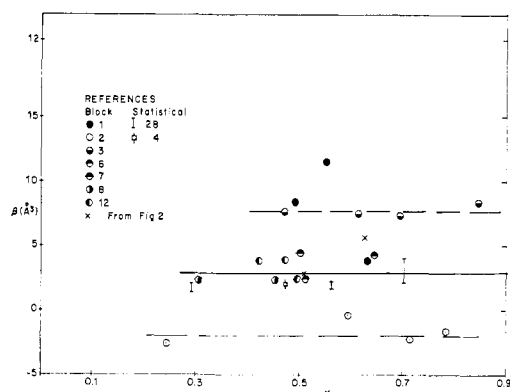


Figure 1. PS-PMMA interaction parameter  $\beta_{12}$  as a function of mole fraction of PS. Points and crosses represent values for block copolymers computed directly (see Table I) and interpolated from Figure 2, respectively. The bars indicate the range of  $\beta_{12}$  computed for statistical copolymers (see Table III) in three solvents. The square represents  $\beta_{12}$  for butanone solution with a standard deviation indicated by the bar.

The quantity of concern here will be the intrinsic viscosity and the basic equation to be used is<sup>13</sup>

$$[\eta]/M^{1/2} = 2.87 \times 10^{21}(A^3 + 0.51BM^{1/2}) \quad (2)$$

This semiempirical relation has been observed to hold<sup>14</sup> for homopolymers in the range  $[\eta]/[\eta]_0 \leq 2.7$ . When using  $M_n$  in eq 2, we found it to be valid also beyond this range.<sup>10</sup>

## Discussion

**A. Block Copolymers.** We consider two series of data. In the first, the solvent and temperature, *viz.* toluene at 25 and 30°, and benzene at 30°, are very similar, especially in respect to polystyrene. In the second, the polymer samples were the same and the solvent was varied.

Table I summarizes the experimental material of the first series. In the sixth column are shown the  $\beta_{12}$ , where 1 and 2 represent styrene and methyl methacrylate, respectively, as computed for each polymer by means of eq 1 and 2, and the characteristic parameters for the two homopolymers, tabulated in Table II. These are derived from results on atactic polymers in the indicated solvents at the temperatures shown. As will be noted,  $\beta$  assumes the identical value for PS in toluene and benzene. Table III exhibits the numerical values of  $\beta_1$ ,  $\beta_2$  and  $\beta_{12}$  in five solvents for two polymer samples in each, one being fractionated, the other as polymerized.<sup>6</sup>

The variation of  $\beta_{12}$  with the mole fraction of PS,  $x$ , shown in Table I, is plotted in Figure 1. There is scatter in the results and the horizontal lines represent crude averages for three apparent groups of points. However, within each group we note the absence of any systematic variation in respect to  $x$ ,  $M$ , numbers of blocks, solvent or temperature. The usual errors in  $[\eta]$  and  $M_n$  are not sufficient to explain the differences in  $\beta_{12}$ . Since all polymers are fractions, differences in

(13) W. H. Stockmayer and M. Fixman, *J. Polym. Sci., Part C*, **1**, 137 (1963).

(14) See, for example, H. Inagaki, T. Miyamoto, and S. Ohta, *J. Phys. Chem.*, **70**, 3420 (1966).

TABLE I  
INTRINSIC VISCOSITIES AND NUMBER AVERAGE MOLECULAR WEIGHTS OF DI- (SM) AND TRI- (MSM) BLOCK COPOLYMERS

No.	$M_n \times 10^{-3}$	$x$	Solvent and temp <sup>b</sup>	$[\eta]/M_n^{1/2} \times 10^3$	$\beta_{12}, \text{\AA}^3$	Ref
1	229	0.631	I	1.73	3.77	1 <sup>c</sup>
2	259	0.550	I	2.83	11.38	1 <sup>c</sup>
3	316	0.490	I	2.54	8.33	1 <sup>c</sup>
4	278 <sup>a</sup>	0.712	II	1.10	-2.33	2
5	529 <sup>a</sup>	0.783	II	1.44	-1.64	2
6	1150 <sup>a</sup>	0.591	II	1.56	-0.32	2
7	2170 <sup>a</sup>	0.243	II	0.95	-2.65	2
8	187	0.470	I	2.05	7.57	3
9	225	0.611	I	2.18	7.45	3
10	302	0.692	I	2.32	7.27	3
11	390	0.845	I	2.40	8.30	3
12	400	0.641	III	2.11	4.29	6 <sup>c</sup>
13	603	0.510	III	1.97	2.47	6 <sup>c</sup>
14	345	0.500	III	2.03	4.47	7 <sup>c</sup>
15	36	0.450	I	1.09	2.20	8
16	37.4	0.302	I	1.05	2.31	8
17	36	0.450	I	1.09	2.20	12
18	317	0.490	I	1.62	2.51	12
19	509	0.420	I	2.05	3.89	12
20	530	0.470	I	2.11	3.89	12

<sup>a</sup>  $M_{app}$  from light scattering. <sup>b</sup> I, toluene, 25.0°; II, toluene, 30°; III, benzene, 30°. <sup>c</sup> Diblocks.

TABLE II  
SHORT- AND LONG-RANGE INTERACTION PARAMETERS FOR PS AND PMMA

No.	Polymer	Solvent	Temp, °C	$a^2, \text{\AA}^2$	$\beta, \text{\AA}^3$	Ref
1	PS	Toluene	25	25.5	2.84	a
2	PMMA	Toluene	25	20.5	1.70	b
3	PS	Benzene	30	25.5	2.84	a
4	PMMA	Benzene	30	20.5	2.28	c
5	PS	Butanone	22	25.5	0.46	d
6	PMMA	Butanone	25	20.5	1.20	e

<sup>a</sup> C. E. H. Bawn, R. J. F. Freeman, and A. R. Kamaliddin, *Trans. Faraday Soc.*, **46**, 1107 (1950). <sup>b</sup> S. N. Chinai, J. D. Matlack, A. L. Resnick, and R. J. Samuels, *J. Polym. Sci.*, **17**, 391 (1955). <sup>c</sup> H.-J. Cantow and G. V. Schul, *Z. Phys. Chem. (Frankfurt am Main)*, **2**, 117 (1954). <sup>d</sup> P. Outer, C. I. Carr, Jr., and B. H. Zimm, *J. Chem. Phys.*, **10**, 830 (1954). <sup>e</sup> F. W. Billmeyer, Jr., and C. B. de Than, *J. Amer. Chem. Soc.*, **77**, 4763 (1955).

TABLE III  
PARAMETERS  $\beta_1$  (PS),  $\beta_2$  (PMMA) AND  $\beta_{12}$  FOR BLOCK COPOLYMERS<sup>6</sup> IN VARIOUS SOLVENTS AT 25°

Solvent	$\beta_1, \text{\AA}^3$	$\beta_2, \text{\AA}^3$	$\beta_{12}, \text{\AA}^3$	$\beta_{12}, \text{\AA}^3$
Benzene	2.13	2.08	4.99	2.93
Chloroform	2.31	3.51	6.52	3.69
Dioxane	1.43	1.96	4.57	2.68
Tetrahydrofuran	1.78	1.39	4.37	2.50
p-Xylene	1.31	-1.25	1.24	0.62

<sup>a</sup> Calculated for unfractionated sample  $M_c = 4 \times 10^5$ ,  $x = 0.641$ . <sup>b</sup> Calculated for a fraction  $M_c = 6.03 \times 10^5$ ,  $x = 0.507$ .

heterogeneity should be of minor importance. The only remaining explanation resides in the structure,

TABLE IV  
 POLYMERIZATION CONDITIONS OF PMMA BLOCKS AND THEIR ESTIMATED TACTICITIES

No.	Initiator	Solvent and temp, °C	Copolymerization	Ref	Tacticity, <sup>a</sup> %			Ref
					<i>i</i>	<i>h</i>	<i>s</i>	
1	PS-OOH	H <sub>2</sub> O (emulsion), 8	PS-OOH purified and dried before second stage of polymerization	1	8	48	44	<i>b</i>
2	Na-PS-Na (initiated by sodium naphthalene)	THF, -78	MMA added to living PS. Gel formed	2	$i + h = 10$		90	<i>c</i>
3	Na-PS-Na (initiated by sodium biphenyl)	THF, -78	Living PS added to MMA. No gel reported	3	$i + h = 10$		90	<i>d</i>
4	PS-K (initiated by phenyl isopropyl potassium + $\alpha$ -methylstyrene tetramer)	THF, -78	MMA added slowly to living PS	6, 7	23	47	30	<i>d</i>
5	$\delta,\delta'$ -Azobis( $\delta$ -cyano-pentanol)	DMF, 100	Homopolymers purified and dried. Coupling by thionyl chloride	8	8	39	53	<i>e-g</i>
6	Anionic polymerization	?	?	12				

<sup>a</sup> Standard deviation  $\pm 5\%$ . <sup>b</sup> Yu. B. Amerik, I. I. Konstantinov, and B. A. Krentsel, IUPAC Macromolecular Chemistry Symposium, Tokyo, Kyoto, Japan, Vol. I, 1966, p 30. <sup>c</sup> R. K. Graham, D. L. Dunkelberger, and E. S. Cohn, *J. Polym. Sci.*, **42**, 501 (1960). <sup>d</sup> R. K. Graham, D. L. Dunkelberger, and J. R. Panchak, *ibid.*, **59**, S43 (1962). <sup>e</sup> C. Walling and D. D. Tanner, *ibid.*, Part A, **1**, 2271 (1963). <sup>f</sup> F. A. Bovey and G. V. D. Tiers, *ibid.*, **44**, 173 (1960). <sup>g</sup> M. Reinmoller and T. G. Fox, *Amer. Chem. Soc., Div. Polym. Chem., Preprints*, **7**, 999 (1966).

*i.e.*, tacticity introduced by differences in the polymerization conditions. These are summarized in Table IV. It is well known that solution polymerization of PS, both radical and anionic, results in conventional atactic polymer, containing *ca.* 80% of syndiotactic diads.<sup>15</sup> In contrast, the tacticity of PMMA depends strongly on the method of synthesis.

The values of  $\beta_{12}$  appear to fall into three groups. The top and bottom lines represent the data of one laboratory each. In Table IV is listed information regarding tacticity as derived from high-resolution nmr spectroscopy of PMMA, prepared under similar conditions as the copolymers used to compute  $\beta_{12}$ . The tacticity of these polymers may be considered comparable to the tacticity of PMMA blocks in the copolymers. From the reported *i*, *h* and *s* indices we obtain a syndiotactic index  $P(s) = s + \frac{1}{2}h$ . A general correlation seems to emerge such that the top and bottom lines in Figure 1 correspond to  $P(s) \simeq 90\%$  whereas for the center line  $P(s)$  fluctuates between 54 and 80% with a standard error of  $\pm 5\%$ . On the other hand,  $h \simeq 5\%$  with the same experimental error for the two extremes, whereas it is distinctly different for the middle group, varying between 39 and 48%.

On the basis of these findings we should not have expected the pronounced difference between the top and the bottom line. The latter encompasses Krause's<sup>2b</sup> data and it is known from earlier work<sup>16</sup> that her polymers have high gel melting points, suggestive of relatively long tactic sequences. This is supported also by the observation<sup>16</sup> that gel forms after 30 min during the copolymerization of the very same samples. If aggregates favored by long-ordered sequences<sup>17</sup> occur intramolecularly, the intrinsic viscosity for a given  $M_w$  and  $\beta_{12}$  in eq 1 and 2 will be reduced. Actually  $\beta_{12}$

is negative in this case. From the difference in  $\beta_{12}$  between the top and the bottom line in Figure 1 we can estimate the change in intrinsic viscosity brought about by this internal aggregation. For molecular weights ranging between  $2.8 \times 10^5$  and  $2.2 \times 10^6$  and  $x$  between 0.24 and 0.78 one finds viscosity ratios between 1.9 and 3.5. In comparison,  $[\eta]/[\eta]_0$  would vary between 2.5 and 5.1 in the absence of aggregation.

The results of Urwin and Stearne<sup>3</sup> are well approximated by the upper line. Judging from the conditions specified, namely, anionic initiation at  $-78^\circ$  in THF, the PMMA block should be highly syndiotactic.<sup>18</sup> The absence of gel in this case may by inference be connected with an absence of long tactic sequences.

The center line groups together polymers initiated either by free radicals<sup>2a,8</sup> or potassium complex<sup>6,7</sup> (1, 4 and 5 in Table IV). As mentioned previously, the heterotactic contents *h* are very similar, and significantly larger than for the other systems. This similarity, however, does not hold in respect to the syndiotactic and isotactic indices. Two samples, namely, 2 and 3 in Table I, depart considerably from the pattern of the other free radical polymers. Both are fractions from a different batch than no. 1 of the same laboratory. We have no interpretation to offer for this apparent discrepancy.

A further correlation results from an examination of the measurements of Dondos, *et al.*,<sup>6</sup> of PS-PMMA copolymers in a series of solvents. The intrinsic viscosities are available for a fraction with  $M_n = 6.03 \times 10^5$ ,  $x = 0.507$ , and for the original preparation with  $M_n = 4.0 \times 10^5$  and  $x = 0.641$ . The authors also provide the intrinsic viscosities of the two homopolymers of a single molecular weight. Using the  $a_i^2$  values in Table II we obtain  $\beta_1$ ,  $\beta_2$  and thus ultimately  $\beta_{12}$  for the five solvents at  $25^\circ$  shown in Table III. Figure 2 indicates a relation between  $\beta_{12}$  and  $\beta_2$ . The upper and lower lines refer to the unfractionated and fractionated copolymer, respectively, and a quite

(18) See Table IV, footnote *d*.

(15) F. A. Bovey, *Polym. Eng. Sci.*, **7**, 128 (1967).

(16) See Table IV, footnote *c*.

(17) H. Z. Liu and Kang-jen Liu, *Amer. Chem. Soc., Div. Polym. Chem., Preprints*, **8**, 982 (1967); A. M. Liquori, G. Anzuino, V. M. Coiro, M. D'Alagni, P. DeSantis, and M. Savino, *Nature*, **206**, 358 (1965).

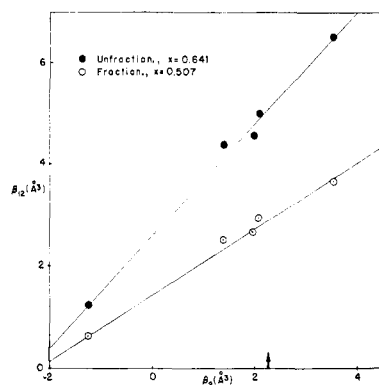
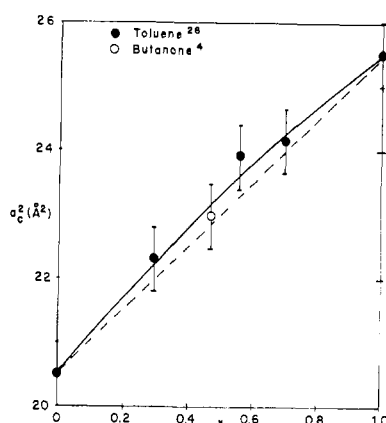


Figure 2. PS-PMMA interaction parameter  $\beta_{12}$  vs. PMMA-solvent interaction parameter  $\beta_2$ , computed from data of ref 6. Open and filled circles represent values for fraction and original unfractionated polymer, respectively. The arrow indicates  $\beta_2$  for PMMA-benzene at 25° (see Table II).



Figures 3. Parameter  $a_c^2$  of PS-PMMA statistical copolymer in toluene (filled circles) and butanone (open circle), 30°, as a function of the mole fraction of PS. The solid line was computed from eq 3 and ref 19. Bars indicate the standard deviation computed from the original  $[\eta]$  — data.<sup>4,19</sup>

accurate linear correlation is found. The differences between the two lines may be caused by the presence of homopolymer in the original batch, as suggested by the authors.<sup>6</sup> An analogous relationship with  $\beta_1$  cannot be observed, since  $\beta_1$  does not vary as much as  $\beta_2$  (see Table III). A similar parallelism between  $\beta_{12}$  and  $\beta_2$  is also noticeable from our styrene (1)-butadiene (2) data.<sup>10</sup>

The arrow marking the abscissa,  $\beta_2 = 2.28$ , corresponds to benzene at 30°, as shown in Table II and used to compute  $\beta_{12}$  in Figure 1. From the two lines we derive  $\beta_{12}$ 's indicated by crosses in Figure 1. The difference between the two points may be taken as a rough measure of the effect of compositional and size heterogeneity on the calculation of  $\beta_{12}$ .

**B. Statistical Copolymers.** Data in several solvents and compositions are at our disposal.<sup>4,19</sup> As before, we start with eq 2 and continue to use the relationship involving  $\beta_c$  (eq 1). However,  $a_c^2$  cannot be expressed as a function of composition by eq 1 (see below). Since a series of molecular weights are available for

(19) T. Kotaka, Y. Murakami, and H. Inagaki, *J. Phys. Chem.*, **72**, 829 (1968). We are indebted to Professor H. Inagaki for a copy of the manuscript prior to publication.

TABLE V  
PARAMETERS COMPUTED FOR RANDOM SM COPOLYMERS

Symbol	$x$	Solvent <sup>a</sup>	$a_c^2$ <sup>b</sup>	$\beta_{12}$ , Å <sup>3</sup>	Ref
SM 3	0.291	I	22.3	$1.98 \pm 0.35$	19
		II	20.7	$2.08 \pm 0.11$	
		III	20.7	$1.26 \pm 0.12$	
SM A <sup>c</sup>	0.474	Butanone	23.0	$1.98 \pm 0.30$	4
SM 5	0.558	I	23.9	$1.67 \pm 0.11$	19
		II	22.7	$1.56 \pm 0.13$	
		II	22.8	$2.08 \pm 0.22$	
SM 7	0.702	I	24.1	$4.00 \pm 0.07$	19
		II	22.2	$2.07 \pm 0.09$	
		III	22.5	$3.25 \pm 0.21$	

<sup>a</sup> I, toluene; II, diethylmalonate; III, 1-chloro-*n*-butane, all at 30°. <sup>b</sup> Standard deviation  $\pm 0.5$ . <sup>c</sup> For  $a_i^2$  and  $\beta_i$  values see Table II.

each composition, least-square treatments of the data for  $[\eta]/[\eta]_0 \leq 2.7$  yield experimental values of  $A_c^2 = a_c^2/M_{0c}$  and  $B_c$  as a function of composition. An analysis of these data has already been presented by the authors<sup>19</sup> themselves. However, they apply a more complicated relation between  $[\eta]$  and  $M$  than eq 2 and assume the unperturbed dimensions to be identical in different solvents and independent of temperature. In Figure 1 are marked the minimum and maximum values of  $\beta_{12}$  for each composition taken from Table V, as well as the range of experimental error for butanone.<sup>4</sup> It is gratifying to note that  $\beta_{12}$  for the statistical copolymers is in the region mapped out by the block copolymers with atactic PMMA segments. Since the parameters  $a_1$  and  $a_2$  are known in toluene, see Table II, we can obtain the dependence of the effective segment length  $a_c$  on  $x$ . The result is shown in Figure 3.

Alternatively a theoretical expression for  $a_i$  is derived from the equation<sup>10</sup>

$$a_c^2 = \sum_{i,j} X_{ij} a_{ij}^2$$

where  $a_{ij}$  refers to an effective segment length determined by an  $i$ - $j$  pair and  $X_{ij}$  is the probability of occurrence of such a pair. The  $X_{ij}$  must be defined strictly in respect to both tactic and chemical placements in the chain. Thus two sets of nearest neighbor, if not higher order, conditional probabilities are involved. The experimental information available is too meager to warrant such a multiparameter effort. Moreover, judging from experimental results on the homopolymers,<sup>20</sup> tacticity appears to have a smaller influence on the unperturbed dimensions than chemical composition. Hence we shall consider only chemical placements, that is, the  $X_{ij}$  will be assumed to be determined entirely by the copolymer composition and the reactivity ratios  $r_1$  and  $r_2$ . The authors<sup>19</sup> give the monomer compositions used in the copolymerization. Since the conversions do not exceed 10%, it is not necessary to use integrated monomer-polymer compositional relationships. For the binary system we write therefore with  $a_{12} = a_{21}$ ,  $a_{ii} = a_i$ ,  $i = 1, 2$

$$(N_1 + N_2)a_c^2 = a_1^2 N_{11} + a_2^2 N_{22} + 2a_{12}^2 N_{12}$$

where  $N_{ij}$ ,  $N_1$ ,  $N_2$  are the number of  $i$ - $j$  pairs, 1's and

(20) I. Sakurada, N. Nakajima, O. Yoshizaki, and K. Nakamae, *Kolloid Z.*, **186**, 41 (1962).

2's in the copolymer, respectively. We have<sup>21</sup>  $N_{ij} = N_i p_{ij}$ , where the conditional probabilities  $p_{ij}$  are given by

$$p_{ij} = 1 - p_{ii}$$

$$p_{ii} = r_i n_i / (r_i n_i + n_j)$$

where  $i, j = 1, 2, i \neq j$ . The monomer composition  $n_i$  is computed from  $N_i$  by means of the relationship

$$N_1/N_2 = n_1(r_1 n_1 + n_2) / [n_2(r_2 n_2 + n_1)] \quad (3a)$$

Hence

$$a_c^2 = a_1^2 x p_{11} + a_2^2 (1 - x) p_{22} + 2x(1 - p_{11}) a_{12}^2 \quad (3b)$$

with

$$x = N_1 / (N_1 + N_2)$$

From Table I of ref 19 we have five sets of data for the determination of the  $r_i$ . In effect only three points are available, since some of the monomer feeds are identical, although the initiator concentration and reaction time were permitted to vary. From the appropriate linear plot of the compositional relationship we obtain  $r_1 = 0.56$ ,  $r_2 = 0.48$ , which compares reasonably well with the tabulated<sup>21</sup> values of  $0.52 \pm 0.03$ ,  $0.46 \pm 0.03$ , or more recently<sup>22</sup>  $r_1 = 0.54 \pm 0.04$  and  $r_2 = 0.42 \pm 0.1$ .

From eq 3 and the values of  $a_c^2$  quoted in Table V for toluene we find  $a_{12}$  to vary between 23.0 and 23.9 for the highest and lowest composition. Since the standard deviation for  $a_c^2$  is  $\pm 0.5$ , an average value of  $a_{12} = 23.5$  is acceptable as a constant to be used in the computation of a theoretical relation between  $a_c^2$  and  $x$ . The result is presented in Figure 3 and we conclude that our analysis, based on eq 3 and copolymerization statistics solely, accounts for the observations as well as can be expected. A nonlinear relationship between the conformational parameter  $\sigma^2 \propto a_c^2$  and  $x$  has been observed previously.<sup>19</sup> Note that  $a_{12}^2$  is close to the mean of  $a_1^2 = 25.5$  and  $a_2^2 = 20.5$ , which may be indicative of particular relationships between the hindrance potentials.

## Conclusion

Our treatment separates the short- and long-range interaction parameters. For block copolymers present experimental data do not permit a direct evaluation of

the former from eq 2 and the additivity of the  $a_i^2$ , eq 1, is employed instead. In the statistical copolymer departures from additivity can be predicted from simple copolymerization theory, eq 3, and directly compared with experiment, using eq 2 for a series of polymers with constant composition. Figure 3 indicates that in the case of PS-PMMA, the deviations from additivity are small.

Having obtained  $a_c$ , one can extract  $\beta_c$  from experiment by means of eq 1. Therefrom the polymer-polymer interaction parameter  $\beta_{12}$  is derived, provided  $\beta_1$  and  $\beta_2$  are known. We have assumed throughout that  $\beta_1$  and  $\beta_2$  depend only on the solvent and temperature but not on the origin of the polymer. This assumption should be satisfactory in respect to  $\beta_1$ , since solution polymerization of styrene is supposed to yield an atactic product. However, there exists experimental evidence that the second virial coefficient in a given solvent is sensitive to tacticity and therefore to the polymerization conditions.<sup>23</sup> Thus variations in  $\beta_2$  cannot be ruled out, but we have no way of estimating the magnitude of the effect in the absence of experimental information for PMMA. The value of  $\beta_2$  adopted corresponds to heterotactic free radical initiated polymer. On this basis one separates three bands of  $\beta_{12}$  values, which could be related to the heterotactic content of the PMMA block. For highly tactic blocks we tentatively suggest an effect of sequence length on  $\beta_{12}$ .

The numerical magnitude of  $\beta_{12}$  for atactic blocks should be least affected by the uncertainties in  $\beta_2$  mentioned above. In the same range are also found the interaction parameters for the statistical copolymers in different solvents. This supports the concept that  $\beta_{12}$  correlates with tacticity. We suggest that the difference between the upper and the center line in Figure 1 is an indication of an enhanced interaction between regularly placed groups. Such an increase would be expected for both syndio and isotactic blocks. Conversely, the position of the bottom line is characteristic of an enhanced interaction between relatively extended  $s$  and  $i$  sequences within the PMMA block.

**Acknowledgment.** This work was partially supported by Contract No. 951836 between the Jet Propulsion Laboratory, California Institute of Technology, and the University of Southern California and sponsored by the National Aeronautics and Space Administration under Contract NAS7-100.

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